

- A camera has a field of view of 90x90 degrees, an image resolution of 400x400 pixels, and that the center of the image is the optical center of the camera. A point P has 3-D coordinates (1m, 2m, 8m) in camera coordinates. Find the pixel projection of point P in the image.
- Solution: we first need to find f. With a fov of 90 degree, f=half the size of the image, or 200 pixels. Then use
 - $x_{img} = f X/Z + c_x = (200)(1m/8m) + 200 = 225$
 - $y_{img} = f Y/Z + c_y = (200)(2m/8m) + 200 = 250$

- A camera views a square lying on a plane; where the plane is parallel to the image plane
 - Show that the width of the square in the image doesn't depend on the location
 - Find the relationship between the width of the square in the image, and the distance to the plane
- Solution
 - Let the plane be a distance Z from the camera
 - Let the sides of the square be at X_1 and X_2 ; $W = X_1 - X_2$
 - The image projection of those sides is $x_1 = f X_1 / Z$, $x_2 = f X_2 / Z$
 - The image width is $w = x_1 - x_2 = f W / Z$

- A CCD sensor is 10mm x 10mm, and has 10M sensor elements. Lens focal length is 6 mm. What is the instantaneous field of view (iFov); ie the angular size of one pixel at the center?
- Solution
 - Assuming the sensor elements are in a square grid, we have $\sqrt{10M}=3162$ elements on a side of 10 mm
 - So one sensor element is $10\text{mm}/3162 = 0.00316$ mm wide
 - At the center, angle is $\text{atan}(.00316/6) = 5.27\text{e-}4$ radian

- What is the IFOV for the human eye? Assume one receptor cell on the retina is .003 mm wide, and the focal length is 17 mm
- Solution
 - $\text{atan}(.003/17) = 1.76\text{e-}4$ radian
- What is width of smallest object you can see at 30m? Assume that the image of the object has to cover at least one receptor cell
- Solution
 - By similar triangles, $w/30\text{m} = .003/17 \rightarrow w = 0.0053$ m